

### MINIMUM MEAN CYCLE ALGORITHM

*Input:* A digraph  $G$ , weights  $c : E(G) \rightarrow \mathbb{R}$ .

*Output:* A circuit  $C$  with minimum mean weight or the information that  $G$  is acyclic.

- ① Add to  $G$  a vertex  $s$  and edges  $(s, x)$  with  $c((s, x)) := 0$  for all  $x \in V(G)$ .
- ② Set  $n := |V(G)|$ ,  $F_0(s) := 0$ , and  $F_0(x) := \infty$  for all  $x \in V(G) \setminus \{s\}$ .
- ③ **For**  $k := 1$  **to**  $n$  **do**:  
    **For** all  $x \in V(G)$  **do**:  
        Set  $F_k(x) := \infty$ .  
        **For** all  $(w, x) \in \delta^-(x)$  **do**:  
            **If**  $F_{k-1}(w) + c((w, x)) < F_k(x)$  **then**:  
                Set  $F_k(x) := F_{k-1}(w) + c((w, x))$  and  $p_k(x) := w$ .
- ④ **If**  $F_n(x) = \infty$  for all  $x \in V(G)$  **then stop** ( $G$  is acyclic).
- ⑤ Let  $x$  be a vertex for which  $\max_{\substack{0 \leq k \leq n-1 \\ F_k(x) < \infty}} \frac{F_n(x) - F_k(x)}{n - k}$  is minimum.
- ⑥ Let  $C$  be any circuit in the edge progression given by  
 $s = p_1(p_2(\cdots(p_n(x))\cdots)), \dots, p_{n-1}(p_n(x)), p_n(x), x$ .

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*Output*  $C$